Air Blast Effects on Structural Shapes

by Graeme Ballantyne, Andrew S. Whittaker, Amjad J. Aref and Gary F. Dargush

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Comprising a consortium of researchers from numerous disciplines and institutions throughout the United States, the Center’s mission is to reduce earthquake losses through research and the application of advanced technologies that improve engineering, pre-earthquake planning and post-earthquake recovery strategies. Toward this end, the Center coordinates a nationwide program of multidisciplinary team research, education and outreach activities.

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A cross-program activity focuses on the establishment of an effective experimental and analytical network to facilitate the exchange of information between researchers located in various institutions across the country. These are complemented by, and integrated with, other MCEER activities in education, outreach, technology transfer, and industry partnerships.

This report investigates the effect of short-duration blast loadings on structural shapes of finite width. A series of numerical analyses on W-shapes are performed using a computational fluid dynamics code. Results such as peak reflected overpressure and reflected impulse are compared to values computed using empirical data reported in the literature for reflecting surfaces of infinite width. Significant reductions in loading are observed. The finiteness of the width dimension allows a low pressure wave to propagate inwards on the front surface of the section, lowering the pressure more quickly than if the section had infinite width. As the blast wave engulfs the section over its width and depth, there is a component of positive pressure on the rear face of the section that opposes the positive pressure on the front surface, which can substantially reduce the net pressure loading below that computed using empirical data. The percentage reduction varies as a function of the size of charge and standoff distance, with the largest reductions observed for small charges and large standoff distances.
ABSTRACT

Following the recent increase in bombings over the last 10 years, blast loading has become a research topic of renewed interest. Many different approaches exist in the design of blast resistant structures, with many designs beginning initially from the simplified hand procedures. Hopkinson and Cranz generated experimental data for key loading parameters such as peak overpressure, arrival time, impulse, and load duration. These parameters are then used to determine a simplified loading history to design the member or structure. A possible oversight of this approach is that the experimental data from which the loading parameters are determined is based on a reflective surface of considerable size, effectively infinite, such as a bomb shelter. Individual structural members however have much smaller widths and could be considered finite surfaces in most scenarios, potentially lowering the loading.

A study was performed to investigate the effect of a W-shape section with finite dimensions on the loading parameters. Two main mechanisms were hypothesized for reducing the loading; ‘clearing’ and ‘wrap-around’. Using the code Air3d, design of experiment procedures and linear regression techniques, a series of analyses were performed. For a given charge mass, held constant for a range of stand-off distances, R, impulse is approximately proportional to 1/R when considering an infinite surface. The impulse when clearing is considered is still proportional to 1/R, however, it is 40-60% lower than the experimental value of impulse, which represents a substantial reduction. The impulse when ‘wrap-around’ can occur is no longer proportional to 1/R but rather 1/R^2. The implications of such a relationship are dramatic, as for a 10 fold increase in R the impulse is 1% of the previous value rather than 10% as the Hopkinson-Cranz data suggests.
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SECTION 1
INTRODUCTION

1.1 Historical Background

Blast engineering and analysis, as with many fields of research, has developed somewhat sporadically over the last sixty to seventy years based upon events throughout this period. Towards the end of World War 2, extensive work was carried out in blast resistant design by government bodies in both the United Kingdom (UK) and United States of America (USA). Particular attention was given to loading effects of nuclear explosions following the deployment of the Hiroshima and Nagasaki atomic bombs. The momentum of this work along with the escalation of the Cold War resulted in continued development in the field of blast engineering amongst government institutions throughout the world. The result of this research was that significant advances were made in structural dynamics and various procedures were developed that were applicable to many structural systems and loading conditions, some of which are documented in Norris et al. (1959) and Biggs (1964).

As well as advances in the structural aspects of blast events, understanding of combustion and explosion phenomena, explosion characteristics and many other effects was greatly improved. Baker et al. (1983) produced a comprehensive text covering many aspects of blast loading.

Despite these advances, attention gradually shifted from blast research to earthquake engineering following a series of damaging earthquakes on the west coast of the USA; including the San Fernando (1971), Loma Prieta (1989) and Northridge (1994) earthquakes, which coupled with the resolution of the Cold War reduced effort in blast engineering research between the early 1980’s and mid 1990’s.

1.2 Recent High Profile Blast Events

Recent or current events play a large role in both academic interest and funding opportunities. In 1992, a bomb was detonated in the financial district of London, UK, close to the Baltic Exchange building at 30 St Mary’s Axe. The Exchange building itself was virtually destroyed and nearby buildings severely damaged, at an estimated cost of $700 million. In 1993, a
terrorist group detonated a 1500lb car bomb below Tower 1 of the World Trade Center (WTC) in the underground parking garage. The blast created a 100ft hole in a number of the sublevel floors while claiming 6 lives and injuring over 1000 people. A few years later, in 1995, a car bomb in Oklahoma City, USA, was detonated next to the Murrah Federal Building that had devastating effects on the Murrah Building and surrounding structures. Over the following ten years, a dramatic increase in terrorist activity saw numerous attacks on influential buildings throughout the world; Canary Wharf, London, UK (1996); Khobar Towers, Khobar, Saudi Arabia (1996); US Embassy, Dar es Salaam, Tanzania (1998); US Embassy, Nairobi, Kenya (1998); World Trade Center, New York, USA (2001); US Consulate, Bali, Indonesia (2002); Jakarta Marriott Hotel, Jakarta, Indonesia (2003); and the Australian Embassy, Jakarta, Indonesia (2004). This heightened terrorist threat saw a substantial increase in blast related research in the USA, UK and Australia.

1.3 Current Methodologies and Standards

Despite research activities for over fifty years, there were very few civilian design standards and documentation that considered blast resistant design. Some guidance was available through US Army Technical Manual TM5-1300 (DOA, 1990), however, after the terrorist attacks on the World Trade Center in 2001, government documentation was subsequently restricted and difficult to obtain. Blast design guidelines were created and textbooks published including the American Institute of Steel Construction (AISC) Blast Guide (AISC, 2005) document produced in 2006 that addresses steel structures. In this guide, individual members are designed as Single Degree of Freedom (SDOF) systems and connections are designed such that redistribution of load is possible. Whilst offering some new direction, many guidelines such as the upcoming ASCE Blast Standard (ASCE, 2007), draw heavily on the work of Norris (1959), Biggs (1964) and Baker et al. (1983).

1.4 Surface Explosions

Many categories of explosions exist: spherical bursts, hemispherical bursts, underwater explosions, internal explosions are a few. The type of explosion considered in this study is a spherical burst from an ideal ‘point’ source.
Most modern explosives can be classed as ideal ‘point’ sources since the chemical compounds used have very high energy densities (i.e. the volume of the domain consumed by the explosive compound is tiny, thus, as far as the surroundings are concerned, the energy comes from a point source) and the speed of reaction is very high such that all the energy is released at almost the same time. The difference between spherical and hemispherical bursts is related to the distance from a large reflective surface.

A spherical burst is an explosion that occurs removed from any reflective surface, for example a device detonated high in the atmosphere. At the time of detonation, a detonation wave front travels out radially through the explosive inducing further detonation of the material. The reaction products are gases at high temperature and pressure that then expand outwards at the shockwave velocity and a layer of compressed air forms in front of the expanding gas as the surrounding air is forced out of the volume it previously occupied. This layer of compressed air is the blast wave and it continues to propagate outwards in a radial fashion from the point source. A hemispherical burst is often the same device as a spherical burst but is located on a large reflective surface such as the ground. The design charts presented for spherical bursts that relate blast wave parameters to scaled distance can be used for hemispherical bursts provided that the mass of the device is increased by a factor of 1.8 for modern high explosives (theoretically, an infinitely rigid reflective surface would magnify the energy by 2 since there would be no energy absorbed by the surface). Baker et al. (1983) provides a thorough treatment of the nature of many explosion types and the characteristics of the corresponding blast waves that are not considered in this study.

1.5 Blast Wave Characteristics

The current method of establishing the pressure loads by hand involves experimental data that provide quantities to define the blast wave such as peak pressure, arrival time, positive duration and positive impulse. After a given arrival time of the shockwave, $t_a$, an instantaneous rise in pressure to the peak value, is observed. The pressure then decays in an exponential manner to ambient in a time interval denoted as the ‘positive phase duration’, $t_d$. Positive phase impulse, $i^+$, is the area below the positive phase portion of the pressure history. Due to overexpansion of the gas surrounding the charge, contraction induces a suction or negative phase that typically is
of much lower magnitude but greater duration than the positive phase. For the purposes of
design, idealized pressure histories are often used that typically ignore the negative phase. Two
main approaches exist; enforce equality of the positive phase impulse (essentially results in a
slightly shorter $t_d$ but actual $i^+$) or assume a linear decay rather than exponential (essentially
results in a larger impulse but actual $t_d$). Figure 1-1 shows a typical blast pressure history,
generated from the Air3d (Rose, 2006) code, at a location away from the burst point and
idealized histories based upon the above discussion.

![Figure 1-1: Actual and Idealized Pressure Histories](image)

**Figure 1-1: Actual and Idealized Pressure Histories** ($R = 6.63m$, $m_{nt} = 14.6$kg, $Z = 2.71m/\sqrt{kg}$)

Throughout the years, experiments have been undertaken and alternative equations proposed to
describe the blast wave quantities, for example; Kingery-Bulmash (1984) (KB) and Hopkinson-
Cranz (HC). Hopkinson (1915) and Cranz (1926) demonstrated that the magnitude of the blast
wave characteristics is proportional to the stored energy of the charge, $E_s$, and the charge stand-
of-f distance, $R$. Common practice in blast engineering is to use a scaled distance $Z$ rather than
the charge stand off, $R$, and is calculated according to equation (1-1) below. In addition to
scaled distance, common practice is to relate the stored energy of any charge to an equivalent
mass of TNT based upon the ratio of the energy densities of the explosives, which is the reason for the mass term in equation (1-1) rather than an energy term.

\[
Z = \frac{R}{\sqrt[3]{m_{\text{eq}}}}
\]  

(1-1)

In equation (1-1), \(m_{\text{eq}}\) is the TNT-equivalent mass. Attention to the unit system is important since \(Z\) in US units is calculated using the weight in pounds of the device rather than the device mass as is the case with SI units. SI units are used throughout this study and conversion factors are provided in Table 1-1 for convenience.

<table>
<thead>
<tr>
<th>Table 1-1: Unit Conversions</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Quantity</strong></td>
</tr>
<tr>
<td>Length</td>
</tr>
<tr>
<td>Mass(^1)</td>
</tr>
<tr>
<td>Force/Weight</td>
</tr>
<tr>
<td>Energy/Moment</td>
</tr>
<tr>
<td>Pressure/Stress</td>
</tr>
<tr>
<td>1 bar</td>
</tr>
<tr>
<td>1 atmosphere</td>
</tr>
<tr>
<td>Scaled Range(^2)</td>
</tr>
<tr>
<td>Mass Density</td>
</tr>
<tr>
<td>Weight Density</td>
</tr>
</tbody>
</table>

1. Mass units of \(\text{lbf} \cdot \text{s}^2 / \text{ft}\) are referred to as ‘slugs’ in the US system.
2. The conversion for scaled range is not a true conversion in the sense that the fundamental units (Length, Mass & Time) are different. \(LM^{-1/3}\) for SI and \(L^{2/3}M^{-1/3}T^{1/3}\) for US since weight is inside the cube-root.
Representation of the blast wave parameters $t_d$, $t_a$, $i^+$ and $P$ can be found in TM5-1300 (DOA, 1990) and Baker et al. (1983) in the form of scaled curves. Figure 1-2, Figure 1-3 and Figure 1-4 show the HC curves plotted on a log-log scale.

Figure 1-2: Scaled Side-on and Reflected Pressure vs. Scaled Distance for Hopkinson-Cranz
Figure 1-3: Scaled Side-on and Reflected Impulse vs. Scaled Distance for Hopkinson-Cranz

Figure 1-4: Scaled Arrival Time and Positive Phase Duration vs. Scaled Distance for Hopkinson-Cranz
Review of Figures 1-2 and 1-3 reveals that there are two traces for pressure and two traces for impulse. The difference between the two traces is related to the interaction of the blast wave with reflective surfaces. As the blast wave approaches the surface it has a side-on pressure, $P_{so}$, that strikes the surface and reflects back, instantaneously increasing the pressure in a process identical to the reflection of a stress wave propagating in a rod. This increased pressure is termed the reflected pressure, $P_r$. Since specific impulse is defined as the area below the pressure history, two impulse traces are presented for side-on and reflective impulse for the same reason. The increase due to the reflection is heavily dependent upon the angle of incidence, $\alpha$, between the wave and the reflecting surface. Figure 1-5 shows the angle of incidence with respect to the reflecting surface. The ratio of the reflected pressure to side-on pressure is termed the reflection coefficient, $C_R$. Figure 1-6 shows the effect of $\alpha$ and $P_{so}$ on the reflection coefficient. The HC curves of Figures 1-2 through 1-4 are based upon $\alpha = 0$ (reflected) and $\alpha = 90$ (side-on).

![Figure 1-5: Angle of Incidence](image-url)
Figure 1-6: Reflection Coefficient vs. Angle of Incidence as a Function of Side-on Pressure (1bar ≈ 14.5 psi), Adapted from Smith and Hetherington (1994)
Theoretical bounds were derived by Rankine and Hugoniot (1870) for normal shocks in ideal gases. Considering, $\alpha = 0$, the peak reflected pressure, $P_r$, is given by

$$P_r = 2P_{so} + (\gamma + 1)q_s$$  \hspace{1cm} (1-2)

where $q_s$ is the dynamic pressure

$$q_s = \frac{1}{2}\rho_su_s^2$$  \hspace{1cm} (1-3)

where $\rho_s$ is the density of the air and $u_s$ is the particle velocity behind the wave front. It can be shown that

$$u_s = \frac{a_0P_{so}}{\gamma p_0} \left[1 + \left(\frac{\gamma + 1}{2\gamma}\right)\frac{P_{so}}{p_0}\right]^{-\frac{1}{2}}$$  \hspace{1cm} (1-4)

where $p_0$ is the ambient pressure, $a_0$ is the speed of sound in air at ambient conditions and $\gamma$ is the ratio of specific heat ($\gamma = 1.4$ for air). Substitution of equations (1-3) and (1-4) into equation (1-2) returns

$$P_r = 2P_{so} \left[\frac{7p_0 + 4P_{so}}{7p_0 + P_{so}}\right]$$  \hspace{1cm} (1-5)

Examination of equation (1-5) reveals that as $P_{so}$ tends towards zero, $C_R$ tends towards 2 ($\alpha = 0$). As $P_{so}$ tends towards infinity, $C_R$ tends towards 8 (this corresponds to a side-on pressure of 48.3 bar when $\alpha = 0$ in Figure 1-6). Further examination of Figure 1-6 reveals that the maximum value of $C_R$ is 12.8 and measured values of 20 have been reported by Smith and Hetherington (1994). These high reflection coefficients occur for very high pressures (small $Z$) and most likely close to the fireball. Here, the air is far from ideal with extreme temperatures, combustion products and dissociation effects (Smith and Hetherington, 1994), which provides a possible explanation for the breakdown of the Rankine-Hugoniot prediction.

### 1.6 Structural Design for Blast Events

Once a pressure history has been established for a given event, the structural system has to be designed to resist the loading. Norris et al. (1959) and Biggs (1964) provide excellent guidance
on the structural design of systems subjected to blast loading. A short overview is discussed here for the reader’s convenience.

Since blast loading is obviously a transient process, the dynamic properties of the system under design are going to influence the response. Consider an elastic single degree of freedom (SDOF) undamped oscillator as shown in Figure 1-7. From elementary dynamics, the natural period of response, $T_n$, for such a system is simply

$$T_n = 2\pi\sqrt{\frac{m}{k}}$$  \hspace{1cm} (1-6)

where $m$ is the mass of the system and $k$ is the spring stiffness. Biggs (1964) demonstrated that the ratio of the loading period, $t_d$, to the natural period of response, $T_n$, was a critical quantity in determining the response of the system. If $t_d$ is less than one-third of $T_n$, the loading can be treated as purely impulsive without introducing significant error. Table 1-2 shows the ratio of $t_d$ to $T_n$ for three common structural shapes and five loading durations.

![Figure 1-7: Elastic Single-Degree-of-Freedom (SDOF) Oscillator](image-url)
Table 1-2: Period ratio for various structural shapes and load durations.¹ ² ³

<table>
<thead>
<tr>
<th>Shape</th>
<th>$t_d$ (msec)⁴</th>
<th>R (m)</th>
<th>$m_{mt}$ (m)</th>
<th>$Z$ (m/kg⁴/³)</th>
<th>$t_d/T_n$</th>
</tr>
</thead>
<tbody>
<tr>
<td>W14 x 193</td>
<td>0.5</td>
<td>0.85</td>
<td>5</td>
<td>0.50</td>
<td>0.03</td>
</tr>
<tr>
<td></td>
<td>1</td>
<td>1.10</td>
<td>5</td>
<td>0.64</td>
<td>0.06</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>1.35</td>
<td>5</td>
<td>0.79</td>
<td>0.11</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>4.50</td>
<td>5</td>
<td>2.63</td>
<td>0.23</td>
</tr>
<tr>
<td></td>
<td>8</td>
<td>25.0</td>
<td>5</td>
<td>14.6</td>
<td>0.45</td>
</tr>
<tr>
<td>W14 x 342</td>
<td>0.5</td>
<td>0.85</td>
<td>5</td>
<td>0.50</td>
<td>0.03</td>
</tr>
<tr>
<td></td>
<td>1</td>
<td>1.10</td>
<td>5</td>
<td>0.64</td>
<td>0.06</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>1.35</td>
<td>5</td>
<td>0.79</td>
<td>0.12</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>4.50</td>
<td>5</td>
<td>2.63</td>
<td>0.24</td>
</tr>
<tr>
<td></td>
<td>8</td>
<td>25.0</td>
<td>5</td>
<td>14.6</td>
<td>0.49</td>
</tr>
<tr>
<td>W14 x 426</td>
<td>0.5</td>
<td>0.85</td>
<td>5</td>
<td>0.50</td>
<td>0.03</td>
</tr>
<tr>
<td></td>
<td>1</td>
<td>1.10</td>
<td>5</td>
<td>0.64</td>
<td>0.06</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>1.35</td>
<td>5</td>
<td>0.79</td>
<td>0.13</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>4.50</td>
<td>5</td>
<td>2.63</td>
<td>0.25</td>
</tr>
<tr>
<td></td>
<td>8</td>
<td>25.0</td>
<td>5</td>
<td>14.6</td>
<td>0.51</td>
</tr>
</tbody>
</table>

1. Shaded cells indicate $t_d/T_n$ less than 0.33, the threshold for impulse loading.
2. Span length for shapes: 6m
4. The values of $t_d$ shown could be obtained using different values of $R$ and $m_{mt}$. The values shown are an example of possible combinations.

In such a loading environment, the response can be determined by imparting an initial velocity which can be calculated as

$$\dot{y}_0 = \frac{i^+}{m}$$

(1-7)
where $\dot{y}_0$ is the initial velocity imparted on the system mass, $m$, due to the impulse, $i^*$. The other condition is when $t_d$ is substantially greater than $T_n$. If $t_d$ is greater than three times $T_n$, the loading can be classed as quasi-static since the inertial resistance of the mass is low. The pressure, $P_R$, then becomes the important loading characteristic in determining the response of the system.

Thus, for a given threat a scaled range can be calculated and the pressure history determined based upon the parameters in Figures 1-2, 1-3 and 1-4. Then the structural system can be designed accordingly, depending upon its own dynamic properties. Generally, the loading duration of a blast event is significantly smaller than the natural period of an element and as a result most structural design for blast events is in the impulsive regime. This implies reduction in impulse would be beneficial for the designer.

1.7 Clearing and Wrap-around

As discussed previously, the majority of the early blast research was concerned with nuclear devices and the global response of structures. As a consequence the HC curves essentially consider an infinite surface, which at a global level is acceptable – design of individual members represents a different problem as the reflecting surface of a column cannot be considered ‘infinite’. Two effects that could alter the parameters obtained from the HC curves are clearing and wrap-around.

1.7.1 Clearing

Clearing is a phenomenon that occurs at the instant the reflected wave reaches the section extremities and is discussed in Norris (1959) and Smith and Hetherington (1994). At the surface extremities, a low pressure wave is generated at the outer corner where vortices are shed as the blast wave passes the front surface. The low pressure shock wave (referred to as a rarefaction wave) races inwards from the surface extremities, accelerating the decay from peak reflected pressure to side-on pressure along the front surface. There will be no reduction in the peak reflected pressure from clearing, however, a reduction in impulse could be observed since the
decay is accelerated by the rarefaction wave depending on how much of the surface the rarefaction wave can reach. Figure 1-8 shows a W section and illustrates the progression of the rarefaction wave along the front face. The rarefaction wave moves at the local speed of sound in the high pressure gas at the head of the rarefaction wave. If the particle flow velocity is high (i.e., close to the point of detonation outside the fireball) and from a region of high pressure to low pressure, the head of the rarefaction wave will propagate slowly and little clearing will be experienced (Ritzel, 2008). Further, pressure loadings within the fireball are due primarily to the ejection of detonation products and the rarefaction wave will not reduce the reflected impulse associated with the ejecta. Some current guidelines provide allowance for clearing (Norris, 1959), based upon an approximate clearing rule

\[ t_c = \frac{3S}{U} \]  

(1-8)

where \( S \) is the clearing distance, which is equal to the half width of the reflecting surface, assuming that the reflecting surface is narrow and tall, and \( U \) is the shock front velocity. Equation (1-8) is based on data collected from shock tube experiments conducted in the 1950s that had an emphasis on far-field pressure loadings from thermonuclear detonations. The utility of this equation for near-field blast loadings of short duration is questionable for near-range detonations that form most of the design threats in urban environments.

1.7.2 Wrap-around

Wrap-around is the ability of the blast wave to wrap around the section and provide a restoring force that opposes the positive impulse on the front face of the section. Consider the exposed W-shape at a stand-off from a device collinear to the axis passing through the web centerline (that is, \( \alpha = 0 \)) shown in Figure 1-9. After a certain time, \( t_1 \), a reflected pressure is experienced on the front face of the front flange as the blast wave propagates outwards. At some time, \( t_2 \),
the wave then engulfs the front flange and the rear face of the front flange experiences a side on pressure, which opposes the reflected pressure acting upon the front face. At time, \( t_3 \), a reflected pressure is experienced by the front face of the rear flange acting in the same direction as the wave propagation. At time, \( t_4 \), a side-on pressure is experienced on the rear surface of the rear flange opposing the reflected pressure on the front face of the rear flange.

![Figure 1-8: Progression of a Shock Wave Around a W-shape Section](image_url)
1.8 Study Objective and Report Organization

1.8.1 Objectives

Two main objectives were identified when this study was undertaken: 1) examination of clearing effects on the pressure histories experienced by structural shapes, specifically the impact on impulse, and, 2) examination of wrap-around effects upon the net impulse experienced by structural shapes subjected to blast loads.

1.8.2 Organization

The following chapter discusses the various techniques and the methodology implemented in conducting the study such as Dimensional Analysis, Design of Experiments, Linear Regression and Numerical Analysis. Section 3 presents the results of the study and the subsequent discussion relating to those results. Conclusions and recommendations that have been drawn based upon the results and discussion are presented in Section 4.
SECTION 2
PROBLEM AND METHODOLOGY

2.1 Problem Definition

To quantify the effects of clearing and wrap around, a study of W-shape sections subjected to blast loading from a spherical charge was carried out with the intention of deriving a relationship between physical parameters and the effect on impulse through clearing and wrap-around. Figure 2-1 shows a schematic of the problem.

Numerical analysis was performed using the Air3d (Rose, 2006) code to generate pressure histories at various locations on the section. Impulse can be calculated through integration of the pressure histories. In order to establish a relationship over a range of scaled distances, several analyses were performed, thus allowing linear regression to be performed to estimate a relationship.

Figure 2-1: Schematic Showing Experimental Layout.
2.1.1 Assumptions and Limitations

As with any research, assumptions are required to simplify complicated events into more manageable problems. Given the complex nature of blast loading there are a number of limitations and assumptions that have been made regarding the numerical modeling, namely,

- Spherical charge (free air burst)
- Fluid-structure interaction has not been considered (i.e. material response of the section has been ignored)
- Thermal effects have not been considered.
- Only the positive phase impulse is calculated.
- Fillets/radii of fabricated/rolled sections have not been included.
- Physical bounds are placed on scaled range.

The suitability of assuming the section behaves rigidly depends upon the ratio of the loading period and natural period of the loaded element. Transient loadings with durations significantly greater than the natural period of the structure can be solved as quasi-static loading without sacrifice of accuracy. Considering a standard W18x35 cross section, with flange thickness of 0.011m, unit flange length and span (outstand) length of 0.076m; the natural period of the flange outstand is 0.65ms. With the exception of events that occur due to a very close satchel type device (small $Z$ and small $m_{in}$) the ratio of loading duration to natural period is going to be large, such that the flange response is significantly slower than the propagation speed of the pressure wave. Clearing occurs when the pressure wave has the opportunity to clear around an object, thus clearing will still be present even if large deformations occur. Secondly, accurate modeling of non-linear fluid-structure interaction at high-strain rates is a computationally extensive procedure and the accuracy of current approaches is questionable. Thus, for the purposes of this study, rigid cross-sections were assumed.

Neglecting the thermal effects of the device is appropriate given the rapid loading duration. The time required for a constantly applied temperature of 1000 degrees on the front and back faces to
increase the flange core temperature by 100 degrees is 0.3secs (Carslaw and Jaeger, 1959), which is orders of magnitude longer than the actual loading duration. This implies that the actual temperature rise in the flange would be insufficient to alter the material properties of the steel. Another thermal effect is the rise in temperature related to internal work of the material. As the section becomes severely deformed, an increase in the material temperature would occur. Due to the rapid nature of the blast loading, in essence the internal work generation is an adiabatic process with around 90% of the work done being converted to heat (Meyers, 1994). Consideration of the temperature rise is pointless since a rigid material assumption has already been made and the increase in deformation due to temperature will likely be small. The thermal effect from internal work was neglected in this study.

Only the positive phase impulse is considered in the analysis for two main reasons. Firstly, a degree of conservatism is retained, which, given the complicated nature of the loading is deemed prudent. Secondly, the values of impulse that we obtain from the HC curves or the KB equations are positive phase impulse.

Since the section has been assumed rigid, there is no benefit in considering the radii of the W-shape section in the numerical analysis. Ignoring the radii in the analysis will have a minimal effect on the overall impulse as they will only affect the pressure histories in the immediate vicinity of the web, which represents a very small proportion of the W-shape cross section.

Finally, physical limitations exist on \( Z \). At low \( Z \), pressures are very high and the loading environment is severe (potentially in the fireball). The applicability of the HC curves begins to break down for a number of reasons. As \( Z \) becomes small, the shape of the charge alters the loadings dramatically. The HC data considers an ideal point source, thus, uncertainty regarding the details of the charge makes simplified hand procedures impractical at small \( Z \). Furthermore, such close-in events will have extremely high pressures causing substantial changes in the cross section that invalidate the modeling assumptions of the analysis and the use of simplified hand procedures for structural design. A scaled range of \( Z = 1m/\sqrt{kg} \) is likely within the fireball based on data presented in Baker et al. (1983), Merrifield and Wharton (2000) and Ritzel (2008), thus the lower limit taken on \( Z \) is approximately \( 1m/\sqrt{kg} \). An upper distance was chosen based
upon a realistic minimum threat at a realistic maximum stand off, that is, the maximum \( Z \) occurs when the smallest charge mass is detonated at the maximum stand off \( Z_{\text{max}} = \left( \frac{R_{\text{max}}}{\sqrt[3]{m_{\text{min}}}} \right) \).

### 2.1.2 Calculation of impulse

Impulse is the integral of the pressure history. To determine the impulse on W-shape cross-sections using the code, the sections were discretized into 44 monitoring areas that had a monitoring point at the centre of each area. The impulse was broken down into 4 main regions. Region 1 represents the front face of the front flange, Region 2 represents the rear face of the front flange, Region 3 represents the front face of the rear flange and Region 4 represents the rear face of the rear flange. Breaking the section surface down into separate regions allows the positive impulse imparted on each region to be determined. Note that the pressure wave loading always opposes the surface normal and consequently the positive phase impulse on each region also acts in the opposite direction of the surface normal. Figure 2-2 shows a diagram of the discretized section identifying the regions and their respective surface normal (\( n_1 \) through \( n_a \)). Note that the problem is symmetric about the centerline of the web, thus, only half the section was modeled.

The net impulse on a region was calculated as an area-average of pressure integrated over time as follows;

\[
i_R^+ = \frac{1}{A_R} \sum_{n=j}^{k} \int_{0}^{t'} A_n p_n(t) dt
\]

where \( i_R^+ \) is the impulse on the region under consideration, \( A_R \) is the area of the region under consideration, \( A_n \) is the tributary area of the \( n \)th monitoring location and \( p_n(t) \) is the pressure history for the \( n \)th monitoring location. Note that the limits of integration imply only the positive phase is included in the calculation, which is consistent with the previous assumptions. The values for \( j \) and \( k \) that define the summation in equation (2-1) are identified below for each region, along with the corresponding definition of \( A_R \). The values increase from left to right as drawn.
For region 1: \( j = 1, \ k = 12, \ A_R = \frac{b_f}{2} \)

For region 2: \( j = 13, \ k = 22, \ A_R = \left(\frac{b_f - t_w}{2}\right) \)

For region 3: \( j = 23, \ k = 31, \ A_R = \left(\frac{b_f - t_w}{2}\right) \)

For region 4: \( j = 32, \ k = 44, \ A_R = \frac{b_f}{2} \)

Figure 2-2: Layout of Monitoring Locations on W-shape for Experiments
2.2 Methodology

Given the volatile nature of explosives, difficulty in accurate instrumentation and the high cost of physical experiments; a numerical study was performed to determine if a reduction in impulse can be expected from clearing and wrap-around. Various techniques were utilized and are described in detail below.

2.2.1 Dimensional Analysis

One of the main problems in any study of this nature is correct identification of the parameters that influence the results. Rather than simply guessing, a more scientific approach was adopted utilizing dimensional analysis (Greenberg, 1988).

Dimensional analysis is frequently used to reduce the number of unknown parameters in a given problem by determining non-dimensional relationships that are a combination of the chosen physical parameters. Familiar quantities derived by these methods can be found in fluid mechanics, for example; Reynolds Number, Mach Number and Biot Number. Dimensional analysis can also be used to determine similitude relations for experiment design.

Review of the problem and a little thought allows an estimation of the parameters that we expect impulse to have a strong dependency on and neglect those which we expect a weak dependency. Table 2-1 shows the chosen variable, symbol and fundamental units (fundamental units being units of Mass, Length and Time).
Once the variables have been chosen, we seek to find all possible dimensionless products of the form:

$$c^\alpha p^\beta E^\gamma V^\delta P^\epsilon i^\zeta b^\phi d^\eta \theta^\kappa = M^0 L^0 T^0$$  \hspace{1cm} (2-2)

Substitution of the fundamental units into equation (2-2) and by equating exponents of M, L and T on both sides we must satisfy the homogenous linear system;

$$\beta + \gamma + \epsilon + \phi = 0$$  \hspace{1cm} (2-3)

$$\alpha - \beta + 2\gamma + 3\delta - \epsilon - \phi + \zeta + \eta = 0$$  \hspace{1cm} (2-4)

$$-\alpha - 2\beta - 2\gamma - 2\epsilon - \phi = 0$$  \hspace{1cm} (2-5)

Equations (2-3), (2-4) and (2-5) represent the mass, length and time exponents respectively. Writing equation (2-3) through (2-5) in matrix form gives;

$$A = \begin{bmatrix} 0 & 1 & 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 1 & -1 & 2 & 3 & -1 & -1 & 1 & 1 & 0 \\ -1 & -2 & -2 & 0 & -2 & -1 & 0 & 0 & 0 \end{bmatrix}$$  \hspace{1cm} (2-6)

Table 2-1: Dimensional Analysis Variables

<table>
<thead>
<tr>
<th>Variable</th>
<th>Symbol</th>
<th>Fundamental Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Speed of sound in medium</td>
<td>$c$</td>
<td>$LT^{-1}$</td>
</tr>
<tr>
<td>Ambient pressure</td>
<td>$p_o$</td>
<td>$ML^{-1}T^{-2}$</td>
</tr>
<tr>
<td>Source energy</td>
<td>$E_s$</td>
<td>$ML^2T^{-2}$</td>
</tr>
<tr>
<td>Volume enclosed by blast wave</td>
<td>$V$</td>
<td>$L^3$</td>
</tr>
<tr>
<td>Side-on overpressure pressure</td>
<td>$P_s$</td>
<td>$ML^{-1}T^{-2}$</td>
</tr>
<tr>
<td>Side-on impulse</td>
<td>$i_s$</td>
<td>$ML^{-1}T^{-1}$</td>
</tr>
<tr>
<td>Width of Flange</td>
<td>$b_f$</td>
<td>$L$</td>
</tr>
<tr>
<td>Depth of Flange</td>
<td>$d$</td>
<td>$L$</td>
</tr>
<tr>
<td>Aspect ratio ($R/b_f$)</td>
<td>$\theta$</td>
<td>$M^0L^0T^0$</td>
</tr>
</tbody>
</table>
\[ \mathbf{x}^T = [\alpha \ \beta \ \gamma \ \delta \ \varepsilon \ \phi \ \zeta \ \eta \ \kappa] \]  \hspace{1cm} (2-7)

\[ \mathbf{C} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \]  \hspace{1cm} (2-8)

and

\[ \mathbf{A} \mathbf{x} = \mathbf{C} \]  \hspace{1cm} (2-9)

Performing Guass elimination of equation (2-9) returns the following solution in terms of \( \chi \);

\[
\mathbf{x} = \begin{bmatrix}
\chi_4 \\
\chi_6 - \chi_5 - \frac{2}{3} \chi_4 + \frac{1}{3} \chi_3 + \frac{1}{3} \chi_2 \\
-\chi_6 - \frac{1}{3} \chi_4 - \frac{1}{3} \chi_3 - \frac{1}{3} \chi_2 \\
\chi_6 \\
\chi_5 \\
\chi_4 \\
\chi_3 \\
\chi_2 \\
\chi_i
\end{bmatrix} \]  \hspace{1cm} (2-10)

By systematically setting each \( \chi \) to 1 and all others to zero, the value of each exponent can be determined allowing derivation of the following dimensionless quantities;

\[ p' = \frac{p_x}{p_o} \text{ when } \chi_1 = 1 \]  \hspace{1cm} (2-11)

\[ i'_x = \frac{c \cdot i_x}{\left(\frac{p_o}{p_o}\right)^{\frac{2}{3}} \cdot \left(E_s\right)^{\frac{1}{3}}} \text{ when } \chi_2 = 1 \]  \hspace{1cm} (2-12)
\[ R' = \left( \frac{p_o \cdot V}{E_s} \right)^{\frac{1}{3}} \text{ when } \chi_3 = 1 \]  
\[ AR = 0 \text{ when } \chi_4 = 1 \]  
\[ b'_f = b_f \cdot \left( \frac{p_o}{E_s} \right)^{\frac{1}{3}} \text{ when } \chi_5 = 1 \]  
\[ d' = d \cdot \left( \frac{p_o}{E_s} \right)^{\frac{1}{3}} \text{ when } \chi_6 = 1 \]  

Examination of equations (2-11), (2-12) and (2-13) reveal very good agreement with the non-dimensional parameters proposed by Sachs (1944). Equations (2-14), (2-15) and (2-16) represent additional parameters that indicate a dependency on the stored energy, ambient pressure and the section dimensions. However, since we are only considering sea level events and assuming that there are no environmental fluctuations in pressure or air density, we need not consider \( p_o \) or \( c \) as they are constants and will not improve a regression model. Equation (2-14) implies a dependency on the ratio of flange width to stand-off. However, given that stand-off and flange width are both already included in equations (2-13) and (2-15), the aspect ratio is not used as a regression variable. In addition, the width-to-depth ratio of typical structural column shapes does not vary significantly. An average ratio was assumed for the purposes of this study, \( d = 1.1b_f \), and equation (2-16) was not considered as a regression variable. From the dimensional analysis, three variables remained; charge mass \((m_{\text{tr}})\), device stand-off \((R)\) and section width \((b_f)\).

### 2.2.2 Design of Experiments

Having established the key variables, it is necessary to determine the variable values at which the experiments should be carried out. Design of Experiments (DOE) is a procedure commonly used in industrial engineering for establishing the variables that effect production rates or product quality.
In the case of this study, the experiments are numerical analysis of a W-shape subjected to blast loading and the values that the charge mass, device stand-off and section width take are determined using DOE methods. In addition to the values that the variables take, DOE methods also dictate the different combination of values that the variables take for each experiment (or analysis run). In DOE literature, variables are known as factors and the variable values are known as factor levels. Montgomery (1991) and Roy (1990) provide information on DOE techniques.

2.2.2.1 Factorial Designs

Methods of experimentation typically revolve around one-factor-at-a-time methods whereby the level of only one factor at a time is changed while all others are held constant. An alternative approach is to use factorial designs. In a factorial design, all possible combinations of the factor levels are considered. The effect of a factor upon the response is said to be the ‘main effect’ of that factor, that is, changing the level (value) of a factor (variable) induces a change in the response. As well as ‘main effects’, the interaction of the factors with each other can have significant consequences on the outcome. By definition, one-factor-at-a-time experiments cannot capture any interaction as all other factors are held constant while one factor is changed. A worked example adapted from Montgomery (1991) is included in Appendix A for completeness.

Factorial designs offer three main advantages over traditional one-factor-at-a-time experiments. Firstly, they are more efficient (relative improvement in efficiency increases with increasing factors). Furthermore, factorial design is necessary when interactions may be present to avoid erroneous conclusions. Lastly, factorial designs allow the effects of a factor to be estimated over several levels of other factors.

2.2.2.2 \(2^k\), \(3^k\) and Central Composite Factorial Design

A specific class of factorial designs and one of the simplest is the \(2^k\) factorial design. Here an experiment with ‘k’ factors (variables) each taking two factor levels (0 and 1, low and high) is run where 0 and 1 represents the lower and upper bounds of a factor. For this study, there are three factors \((m_{in}, b_f, R)\) and the required number of analysis to complete the study is eight \((2^3)\).
A restriction on a $2^k$ design is that only linear relationships can be predicted, that is, only linear interactions between factors can be observed as the levels represent the extremes of the applicable ranges. As the factors each take only two levels then it is not possible to predict any curvature in the response (you can only fit a straight line through two points). The logical step is to design a $3^k$ experiment, ‘$k$’ factors at three levels (-1, 0 and 1), thus providing a midpoint that would allow to check for curvature.

Orthogonality is an important concept of factorial designs. Orthogonality is the optimal design criterion as it minimizes the variance of the regression coefficients. The attractiveness of this property is that the response is only a function of the distance from the design centre and not the direction (function of only $R$ not $\theta$ if considering a polar co-ordinate system). It therefore makes sense to use an experimental design that provides equal precision of estimation in all directions. In using a $3^k$ design, the attractive feature of orthogonality is lost as $3^k$ designs are not ‘orthogonal’. Thus $3^k$ models exhibit a degree of bias depending upon the direction.

Clearly a design that retains the attractive property of orthogonality and has the ability to test for curvature (nonlinearity) is desirable. One classification of design that meets these requirements is a central composite design (CCD). Figure 2-3 shows a schematic representation of a CCD for $k = 2$. The axes in the figures represent the factors (variables) and each point represents an experiment in the design with the location along the axes relating to the factor level (variable values). By careful selection of the level $\alpha$ and the number of center points, points with co-ordinates $(0,0)$ in Figure 2-3, an experiment can be designed based upon the $2^k$ factorial design that tests for curvature and meets the orthogonality condition. Setting $\alpha = \sqrt[4]{2^k}$ ensures an orthogonal design (Montgomery, 1991). In a CCD design however, the extremes are no longer represented by -1 and 1 but by $-\alpha$ and $+\alpha$. 
2.2.2.3 Factors, Levels and Matrix of Experiments

The three factors considered here are charge mass, device stand-off and flange width. The factorial design chosen was an $2^k$ orthogonal central composite design with $k = 3$ and $\alpha = 1.682$. Table 2-2 contains the bounding values for the factors that are selected based upon realistic bounds on the physical problem.

The range of $b_j$ was chosen based upon the minimum (0.3m) and maximum (0.5m) section widths commonly used in practice. The range of $m_{mt}$ was determined based upon a 5kg satchel device being the minimum charge mass and a 1000kg vehicle device being the maximum. The range on stand-off was decided based upon limits on scaled distance, with 3m being the minimum before scaled range became too small and 150m being a practical maximum.

The upper and lower bounds chosen for both stand-off and charge mass vary by orders of magnitude. In addition, from dimensional analysis, pressure and impulse vary with the inverse of the cube root of the mass rather than the mass. Although the CCD design can predict curvature, to obtain best results, the range was made as linear as possible. By taking the logarithm of the
bounds for stand-off and inverse of the cube root of mass, more linear ranges were achieved. The factor levels corresponding to $-\alpha$, -1, 0, 1, $+\alpha$ were determined based upon the modified bounds and are presented in Table 2-3. Manipulation of these factor levels was required to obtain the physical values as input to the Air3d code. Table 2-4 shows the matrix of experiments demonstrating the various combinations of factors and levels for the analysis. It should be noted that although DE procedures were used for experiment design, it became apparent from the results of analysis that variable interaction was minimal.

<table>
<thead>
<tr>
<th>Table 2-2: Bounding Values for $b_f$, $R$ &amp; $m_{nt}$</th>
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<tbody>
<tr>
<td><strong>Factor</strong></td>
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<td>-----------------------------------------------</td>
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<tr>
<td>Flange width, $b_f$</td>
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<tr>
<td>Stand-off, $R$</td>
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<td>Charge mass, $m_{nt}$</td>
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<th>Table 2-3: Factor Levels</th>
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<tr>
<td><strong>Factor Levels</strong></td>
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<td>-----------------------------------------------</td>
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<tr>
<td>Flange width, $b_f$</td>
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<tr>
<td>Stand-off, $\log(R)$</td>
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<tr>
<td>Charge mass, $-0.33\log(m_{nt})$</td>
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<td>Run</td>
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</table>
2.2.3 Numerical Analysis

Numerical analysis was utilized to solve the matrix of experiments defined by DOE procedures. Numerical analysis presents various advantages over conventional experimentation provided that the algorithms involved are accurate, reliable and robust. Firstly, the cost associated with multiple tests is significantly less for numerical approaches than experimental methods. Secondly, more scenarios can be investigated allowing a better understanding of the problem. Finally, more information can be obtained from numerical methods as it is very difficult to instrument an experiment in a similar level of detail. Also, in the case of localized effects due to blast loading, it is highly unlikely that an experiment can be designed such that results other than qualitative can be obtained due to the small sampling rates, extreme deformations and volatile environmental conditions from the fireball.

2.2.3.1 Air3D Methodology

The numerical code used was Air3d (Rose, 2006), developed by Dr. Timothy Rose of Cranfield University specifically for examining the effects of blast waves on structures. The code solves the differential Euler equations of fluid mechanics, the tensorial representation is shown below in equation (2-17), using a finite difference method in both space and time.

\[
\frac{\partial \rho}{\partial t} + \frac{\partial \rho u}{\partial x} = 0 \tag{2-17}
\]

\[
\frac{\partial \rho u}{\partial t} + \frac{\partial}{\partial x} (\rho u^2 + p) = 0 \tag{2-18}
\]

\[
\frac{\partial \rho}{\partial t} \left( e + \frac{u^2}{2} \right) + \frac{\partial}{\partial x} \left( \rho u^2 + p \right) = 0 \tag{2-19}
\]

where \( \rho \) is the fluid density, \( u \) is the fluid velocity, \( p \) is the fluid pressure, \( e \) is the internal energy per unit mass for the fluid, \( \partial/\partial t \) is the partial derivative with respect to time and \( \partial/\partial x \) is the partial derivative with respect to space. Validation of Air3D was made using the HC curves. Results are shown in Figures 2-4 through 2-8. It is clear that Air3D provides good correlation with the HC data for the cases of side-on and reflected waves, predicting the general trends extremely well. The impulse calculated by Air3d is consistently lower than the HC values when
$Z > 2$, generally in the region of 15-20% less. Although not matching exactly, Air3d predicts the trends very well and given the uncertainty of blast loading and age of the HC data, a 20% difference is not unreasonable.

Figure 2-4: Comparison of Air3d Side-on Pressure with Hopkinson-Cranz Data

Figure 2-5: Comparison of Air3d Side-on Impulse with Hopkinson-Cranz Data
Figure 2-6: Comparison of Air3d Arrival Time with Hopkinson-Cranz Data

Figure 2-7: Comparison of Air3d Reflected Pressure with Hopkinson-Cranz Data
Air3d treats 3D analysis in a multi-stage process, whereby the 1D domain is solved then mapped to the 2D domain which in turn is solved before being mapped to 3D domain if required. The dimensionality of the analysis depends upon the input data provided, that is, only 1D input should be provided if a 1D analysis is required, 1D and 2D data should be provided if a 2D analysis is required and 1D, 2D and 3D data should be provided if the 3D analysis is required.

Each stage of an analysis uses a constant cell size specified by the user, although the cell size between stages can be different. The author of Air3d recommends a scaled cell size of $1 \times 10^{-3} \text{m}^{1/3} \text{kg}^{-1/3}$ for the 1D analysis to accurately capture the detonation process over a range of $Z$. No cell size is recommended for the subsequent analysis as it is largely controlled by the computational demand although the jump in cell size between 1D to 2D or 2D to 3D will affect the accuracy of the mapping procedure. Only 2D analysis were performed in this study with the scaled cell sizes for 1D and 2D analysis of $5 \times 10^{-4} \text{m}^{1/3} \text{kg}^{-1/3}$ and $2.5 \times 10^{-3} \text{m}^{1/3} \text{kg}^{-1/3}$ respectively.

**Figure 2-8: Comparison of Air3d Reflected Impulse with Hopkinson-Cranz Data**
Air3d generates a domain based upon outer dimensions specified by the user, which then is
discretized based upon the cell size (obtained by multiplying the scaled cell size with the cube
root of the charge mass) specified for that stage of analysis. In addition to the domain
dimensions the charge mass is required to determine the initial energy of the analysis.

Reflective objects can be defined by creating geometric obstacles that void any cells whose
midpoint is bounded by the obstacle edges and prevents their inclusion in the calculation,
essentially behaving as a rigid surface. The W-shape sections were created in this manner.

Data output can be defined by specification of monitoring locations in the domain; Air3d can
output both temperature and pressure histories. In order to define a monitoring location, the user
specifies the co-ordinates of the desired monitoring locations in the domain for which Air3d
outputs the data. The data from a monitoring location is analogous to pressure transducers or
thermocouples in the sense that no knowledge of the surface normal is included in the data, only
a measure of pressure or temperature. Thus the direction of impulse was assigned to the data
manually to coincide with the surface normals.

2.2.4 Linear Regression Analysis

Linear regression analysis is a technique where observations are approximated using an assumed
function and the quality of the prediction or ‘goodness of fit’ is assessed using statistical
methods. Linear Regression is covered in many texts, for example, Montgomery (1991) and
Soong (2004) although a brief outline is presented below. The simplest case of linear regression
is when the observations are believed to be dependent upon only one variable.

2.2.4.1 Least-Squares Method of Estimation

Assuming that the random variable $Y$ is a function of only one independent random variable $x$
and their relationship is linear, that is

$$Y = \alpha + \beta x + \epsilon$$

(2-18)
where $\alpha$ and $\beta$ are regression coefficients and $\varepsilon$ is the residual error. Using the least-squares method, estimation of $\alpha$ and $\beta$ seeks to minimize the sum of the squared residuals. Consider the set $(x_1, Y_1), (x_2, Y_2), \ldots, (x_n, Y_n)$, rearranging equation (2-18) yields

$$\varepsilon_i = \hat{\alpha} + \hat{\beta}x_i - Y_i$$ \hspace{1cm} (2-19)

where $\hat{\alpha}$ and $\hat{\beta}$ are estimates of the regression parameters and $\varepsilon_i$ is the residual at $(x_i, Y_i)$. Minimization of the sum of the squared residuals allows us to estimate the regression coefficients as,

$$\hat{\alpha} = \bar{Y} - \hat{\beta}\bar{x}$$ \hspace{1cm} (2-20)

$$\hat{\beta} = \left[ \sum_{i=1}^{n} (x_i - \bar{x})(Y_i - \bar{Y}) \right] \left[ \sum_{i=1}^{n} (x_i - \bar{x})^2 \right]^{-1}$$ \hspace{1cm} (2-21)

Although the example presented considers only one variable, the process is identical for multivariable regression by simply including another regression coefficient for each random independent variable on which random variable $Y$ depends. It is important to note that linear regression analysis provides meaningless results if the relationship between the random variable $Y$ and the independent random variables is anything other than linear, even if a straight line appears to provide a good ‘fit’. 

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SECTION 3
ANALYSIS, RESULTS AND DISCUSSION

3.1 Analysis

An analysis was performed using Air3d (Rose, 2006) for each of the 20 runs in the matrix of experiments presented in Table 2-4. Pressure histories were output for the 44 monitoring locations, which were manipulated using Matlab (Mathworks, 2004) to obtain averaged pressure histories for each of the defined regions. Region 1 comprises the front face of the front flange, region 2 the rear face of the front flange, region 3 the front face of the rear flange and region 4 the rear face of the rear flange (see Figure 2-2). The advantage of breaking down the cross section in this fashion is that it permits examination of the influence of the average pressure history acting on each region.

3.2 Results

This results section is divided into two parts: 1) the results of the numerical analysis, and 2) the results of the linear regression analysis. In all results, any reference to pressure is an overpressure, that is, relative to the ambient pressure.

Four different measures were used to examine different conditions. Measure 1 considered the monitoring location in region 1 that lay closest to the web centerline. If clearing was not present then this pressure history should return the same value of reflected impulse as the HC curves since Air3d and the HC curves for an infinite surface yield identical results (see Chapter 2). Measure 2 considered the average pressure history over region 1, thus giving a measure of the effect of clearing on reflected impulse. Measure 3 considered the effect of wrap around on the open section (region 1 - region 2 + region 3 - region 4), to obtain the net pressure history on the open section. The average pressure histories of all regions were summed in Matlab, based upon their surface normal to compute measure 3. Measure 4 considered wrap-around of a closed (tubular) section with the same width and depth as the open sections. This was achieved by considering only the average pressure histories of regions 1 and 4, again summed based upon their surface normal (region 1 - region 4). In this measure, it was assumed that the effect of the open section does not significantly affect the pressure histories in region 4 (see Appendix B for
Figure 3-1 compares the average pressure history for region 4 of a W-shape (neglecting the contribution of regions 2 and 3) and for a RHS of the same outer dimensions, for one of the validation cases of Appendix B. Clearly, there is minimal effect on the average pressure history. The net reflected impulse imparted on the section for each measure was obtained by integration of the pressure histories with respect to time. The results were then compared to the HC values of reflected impulse.

The validation) and therefore allows an estimation of the effect of ‘encasing’ open sections. Figure 3-1 compares the average pressure history for region 4 of a W-shape (neglecting the contribution of regions 2 and 3) and for a RHS of the same outer dimensions, for one of the validation cases of Appendix B. Clearly, there is minimal effect on the average pressure history.

The net reflected impulse imparted on the section for each measure was obtained by integration of the pressure histories with respect to time. The results were then compared to the HC values of reflected impulse.

![Figure 3-1: Comparison of the Average Back Face Pressure History for W-shape and RHS sections for $R = 6.63\text{m}$, $m_{int} = 14.6\text{kg}$ and $Z = 2.71\text{m/s/roots(kg)}$ with Section Outer Dimensions $b_j = 0.459\text{m}$, $d = 0.505\text{m}$](image)

### 3.2.1 Numerical Analysis Results

Figure 3-2 and 3-3 overlay the average pressure histories per region and the pressure histories for each measure for a typical analysis, respectively. Figure 3-2 appears to have many additional peaks in the pressure histories, which is initially counter-intuitive. However, the individual histories can be explained by consideration of the interaction of the blast wave with the W-shape section. Consider the pressure histories for regions 1 and 4; both exhibit a single peak and decay to 0kPa (note that 0kPa overpressure corresponds to atmospheric pressure), which is the
expected profile for a blast wave. However, the pressure histories in regions 2 and 3 contain multiple peaks that appear to be out of phase. This is due to reflection from the flanges. As the wave engulfs the front flange, the rear face of the front flange experiences a side-on pressure (the first peak in the pressure history for region 2). The wave then propagates towards the rear flange, striking the front face of the rear flange that experiences a reflected pressure (the first peak in the pressure history for region 3). This reflected pressure wave then propagates back towards the front flange striking the rear face of the front flange as a reflected pressure causing the second peak in region 2’s pressure history (which has a higher magnitude than the first peak). Meanwhile, the initial wave has engulfed the rear face of the rear flange, thus region 4 experiences a side-on pressure. Region 1 and 4 demonstrate typical profiles for a blast wave because they are not subjected to the repeated reflections that regions 2 and 3 experience from the wave reflecting back and forward between the flanges.

The region 1 peak reflected pressure, arrival time and load duration from Figure 3-2 is 255kPa, 8msec and 4.5msec respectively. For $Z = 2.17 m^{3/2}/\sqrt{\text{kg}}$ and $m_{int} = 14.6 \text{ kg}$ the HC curves give 282kPa, 7.5msec and 5.7msec for reflected pressure, arrival time and load duration which gives percentage differences of 9.6%, 6.3% and 21.0%. Although the difference is between 5 - 20% (for the particular scaled distance and charge mass under consideration), given that there is an averaging process being performed and clearing effects are included the values are clearly of the correct order.

The side-on pressure for $Z = 2.17 m^{3/2}/\sqrt{\text{kg}}$ from the HC curves is 86.8kPa (0.87bar), which gives a reflection coefficient of 2.94 based upon a peak reflected pressure of 255kPa. The reflection coefficient from Figure 1-6 for a side-on pressure of 0.87bar and $\alpha = 0$ is approximately 2.7. These comparisons, whilst not yielding exact agreement demonstrate that the Air3d results are of the correct order. A more involved validation of the calculated measure values is contained in Appendix B.
Figure 3-2: Sample Average Pressure Histories for Each Region for $R = 6.63 \text{ m}$, $m_{nt} = 14.6 \text{ kg}$ and $Z = 2.71 \text{ m/} \sqrt{\text{kg}}$

Figure 3-3: Sample Pressure Histories for each Measure for $R = 6.63 \text{ m}$, $m_{nt} = 14.6 \text{ kg}$ and $Z = 2.71 \text{ m/} \sqrt{\text{kg}}$
Figure 3-3 presents interesting findings regarding the individual measures. The histories for measure 1 and 2 are almost identical indicating that effect of clearing is constant along the flange width (for the given charge mass, stand-off and flange width). Measure 3 and 4 both have significant regions of negative impulse opposing the positive impulse from region 1, suggesting that the net impulse for these measures will be substantially lower.

Figures 3-4 through 3-7 show the reflected impulse for each measure and the HC reflected impulse plotted against scaled distance. All 20 analyses from the matrix of experiments are plotted, although there appears to be fewer data points in Figure 3-4. This is related to the scalability of impulse; many of the analyses share identical values of $Z$. Thus as the scaled impulse is the same for any given $Z$, the data points lie exactly on top of each other (note also that runs 16 – 20 in the matrix of experiments are identical and as such the results are identical also). As can be observed from the figures, all points are below the HC curves, therefore reduction in impulse from that predicted by the HC curves is present in all measures.

In Figure 3-4, there appears to be only 9 data points. As explained above, this is because a number of analyses share a common value of $Z$ and the flange width does not affect measure 1 as only one monitoring location at the center of the flange is considered. Figure 3-5, however, has 15 data points indicating that the flange width does have an effect on the averaged pressure history and subsequently the impulse. Measure 1 and 2 are both approximately proportional to $1/Z$.

Figures 3-6 and 3-7 have the 15 data points, again because flange width is included in the calculation of impulse. The effect of flange width is small compared to the negative impulse portions for these measures, which was highlighted in the discussion of Figure 3-3. Measures 3 and 4 appear to be approximately proportional to $1/Z^2$ rather than $1/Z$ as is the case for measures 1 and 2.
Figure 3-4: Comparison of Measure 1 to HC Reflected Impulse vs. Scaled Distance

Figure 3-5: Comparison of Measure 2 to HC Reflected Impulse vs. Scaled Distance
Figure 3-6: Comparison of Measure 3 to HC Reflected Impulse vs. Scaled Distance

Figure 3-7: Comparison of Measure 4 to HC Reflected Impulse vs. Scaled Distance
The reflected impulse reduction factor, relative to the HC curves, is shown in Figures 3-8 through 3-11, and is defined as

\[ \eta_n = \frac{i_n^+}{i_{HC}^+} \]  

(3-1)

where \( \eta_n \) is the reduction factor for the \( nth \) measure, \( i_n^+ \) is the net reflected impulse for the \( nth \) measure and \( i_{HC}^+ \) is the positive impulse from the HC curves (that do not consider clearing effects).

Figures 3-8 and 3-9 indicate that for measures 1 and 2 the reduction factor is constant over a wide range of scaled distance, where \( \eta_1 \) and \( \eta_2 \) average around 50%.  Figures 3-10 and 3-11, however, indicate significant reductions in reflected impulse with respect to HC with increasing scaled distance.  For \( Z \) larger than \( 11m/\sqrt{kg} \) the reduction factor is approximately 0.02 that suggests for measure 3 and 4 the impulse will be 2\% of the HC reflected impulse that does not account for either clearing or wrap-around.

As described previously, measure 3 considers a W-shape section subject to wrap around and measure 4 considers a rectangular hollow section with the same outer dimensions as the W-shape.  Figures 3-12 and 3-13 plot the ratio of \( \eta_1 \) to \( \eta_2 \) and \( \eta_3 \) to \( \eta_4 \), respectively.  Figure 3-12 reveals that \( \eta_2 \) is always smaller than \( \eta_1 \) and that the ratio approaches unity as \( Z \) increases.  This would be expected as \( \eta_2 \) includes the effect of clearing at the flange extremities, whereas, \( \eta_1 \) considers the pressure history at the web centerline that will experience smaller clearing effects.

Figure 3-13 shows that \( \eta_3 \) is always larger than \( \eta_4 \) and in general, \( \eta_3 / \eta_4 \), increases with increasing \( Z \).  This would be expected as measure 3 has a two reflective faces compared to measure 4’s single reflective surface.  Figure 3-14 shows a plot of the difference between the
reduction factors for measures 3 and 4, defined in equation (3-2) below, which can help the reader identify the impact of open versus closed sections.

\[ \delta \eta = \frac{i_3^+ - i_4^+}{i_{HC}^+} = \eta_3 - \eta_4 \]  

(3-2)

Figure 3-14 reveals that as \( Z \) increases the benefit of closing or encasing a column section becomes smaller, as the difference between the measure 3 and 4 impulses becomes small relative to the HC impulse. Thus, despite Figure 3-13 showing that \( \eta_3 \) is approximately a factor of 1.6 greater than \( \eta_4 \) when \( Z = 20 \text{ m}/\sqrt[3]{\text{kg}} \), Figure 3-14 shows that for \( Z > 10 \text{ m}/\sqrt[3]{\text{kg}} \) the benefit is only an additional 1% of the HC impulse. Given that \( \eta_3 \) is around 3% of the HC value for \( Z > 10 \text{ m}/\sqrt[3]{\text{kg}} \), the benefit of encasing W-shape sections is likely small.

![Figure 3-8: Measure 1 Reduction Factor, \( \eta_1 \), vs. Scaled Distance](image)

Figure 3-8: Measure 1 Reduction Factor, \( \eta_1 \), vs. Scaled Distance
Figure 3-9: Measure 2 Reduction Factor, $\eta_2$, vs. Scaled Distance

Figure 3-10: Measure 3 Reduction Factor, $\eta_3$, vs. Scaled Distance
Figure 3-11: Measure 4 Reduction Factor, $\eta_4$, vs. Scaled Distance

Figure 3-12: $\eta_1/\eta_2$ vs. Scaled Distance
3.2.2 Linear Regression Results

Linear regression analysis was performed on the data to determine relationships between reflected impulse \( (i^+) \), scaled distance \( (Z) \) and scaled flange width \( (l = b_f / \sqrt{m_{in}}) \). The
selection of scaled distance and scaled flange width as regression variables came from the dimensional analysis performed in Chapter 2, the general form of the regression equation utilized is shown below in equation (3-3).

\[ \hat{y} = 10^{\hat{\beta}_0} x_1^{\hat{\beta}_1} x_2^{\hat{\beta}_2} \]  

(3-3)

Taking the logarithm of equation (3-2) yields the following relationship;

\[
\log_{10}(\hat{y}) = \hat{\beta}_0 + \hat{\beta}_1 \log_{10}(x_1) + \hat{\beta}_2 \log_{10}(x_2)
\]

(3-4)

Equation (3-3) demonstrates that when plotted on a log-log scale, the regression parameters \( \beta_1 \) and \( \beta_2 \) represent the slope of the line \( \hat{y} \) with respect to \( x_1 \) and \( x_2 \). Equations (3-5) through (3-15) below show the regression equations for the measures previously defined.

\[ i_1^* = 10^{2.483 \cdot 0.017 Z^{-1.162}} \]  

(3-5)

\[ i_2^* = 10^{2.438 \cdot 0.001 Z^{-1.138}} \]  

(3-6)

\[ i_3^* = 10^{2.790 \cdot 0.338 Z^{-2.271}} \]  

(3-7)

\[ i_4^* = 10^{2.574 \cdot 0.290 Z^{-2.297}} \]  

(3-8)

\[ \eta_1 = 10^{-0.312 \cdot 0.001 Z^{-0.027}} \]  

(3-9)

\[ \eta_2 = 10^{-0.356 \cdot 0.017 Z^{-0.003}} \]  

(3-10)

\[ \eta_3 = 10^{-0.005 \cdot 0.320 Z^{-1.137}} \]  

(3-11)

\[ \eta_4 = 10^{-0.220 \cdot 0.272 Z^{-1.163}} \]  

(3-12)

\[ \eta_1/\eta_2 = 10^{0.044 \cdot 0.016 Z^{-0.024}} \]  

(3-13)

\[ \eta_3/\eta_4 = 10^{0.216 \cdot 0.048 Z^{0.026}} \]  

(3-14)

\[ \delta\eta = \eta_3 - \eta_4 = 10^{-0.464 \cdot 0.379 Z^{-1.080}} \]  

(3-15)

As previously mentioned, the exponents in equations (3-4) through (3-15) represent the slope of the each equation in the log-log space (can also be thought of as the proportionality), thus given
the small contribution of scaled flange width, DE procedures were not used to investigate variable interaction. Consider the value of the exponent on $Z$ for equations (3-5) through (3-8). The values confirm the observation made earlier that the reflected impulse for measures 1 and 2 is approximately proportional to $1/Z$ whereas for measures 3 and 4, the reflected impulse is proportional to $1/Z^2$.

Figures 3-15 through 3-25 show the linear regression trendlines fitted through the numerical analysis data presented above in Figures 3-4 through 3-14. Three trendlines are plotted in each figure. The light gray dashed line represents the maximum scaled flange width which was calculated as the largest flange width (0.5m) divided by cube root of the minimum charge mass (5kg), hence, $l_{\text{max}} = 0.5/\sqrt[3]{5} = 0.29 \text{ m/}^{\frac{3}{2}}\text{kg}$. The dark gray dashed line represents the minimum scaled flange width which was calculated as the smallest flange width (0.3m) divided by cube root of the maximum charge mass (1000kg), hence, $l_{\text{min}} = 0.3/\sqrt[3]{1000} = 0.03 \text{ m/}^{\frac{3}{2}}\text{kg}$. The light gray solid line represents an average scaled flange width, which was calculated as the average of the maximum and minimum scaled flange widths, hence, $l_{\text{mean}} = (0.29 + 0.03)/2 = 0.16 \text{ m/}^{\frac{3}{2}}\text{kg}$. The solid black line shown in Figures 3-15 through 3-18 represents the HC impulse, which is included for comparison. It should be noted that linear regression should not be used for extrapolation, thus $l_{\text{max}}$ and $l_{\text{min}}$ represent the upper and lower bounds on the scaled flange width. Equations (3-4) through (3-15) are only valid for scaled distance $1 \text{ m/}^{\frac{3}{2}}\text{kg} \leq Z \leq 30 \text{ m/}^{\frac{3}{2}}\text{kg}$. 
Figure 3-15: Comparison of Measure 1 Trendlines to HC Reflected Impulse

Figure 3-16: Comparison of Measure 2 Trendlines to HC Reflected Impulse
In most figures, all data points are bounded by the maximum and minimum values of scaled flange width. The reduction factor trendline is essentially constant for measures 1 and 2 for both scaled distance and flange width, which is confirmed in Figures 3-19 and 3-20 (the percentage difference between the measure and HC reflected impulse is constant). Figures 3-21 and 3-22
show that the reduction factors for measure 3 and 4 have the same slope as that of the HC reflected impulse. This is related to the relative magnitude of the $Z$ exponents for the measures and the HC reflected impulse. This can easily be demonstrated by considering equations (3-6) and (3-7), from which;

$$i_{HC} \propto Z^{-1.15} \quad (3-14)$$

$$i_{3,4}^+ \propto Z^{-2.30} \quad (3-15)$$

The reduction factor, $\eta$, which has been defined earlier as the ratio of the Air3d reflected impulse to the HC reflected impulse, see equation (3-1), is therefore proportional to;

$$\eta_{3,4} \propto Z^{-2.30} \frac{Z^{-1.15}}{Z^{-1.15}} \propto Z^{-2.30 - (-1.15)} \propto Z^{-1.15} \quad (3-16)$$
Figure 3-19: Reduction Factor, $\eta_1$, Trendlines

Figure 3-20: Reduction Factor $\eta_2$ Trendlines
Figure 3-21: Reduction Factor $\eta_3$ Trendlines

Figure 3-22: Reduction Factor $\eta_4$ Trendlines
Figure 3-23: $\eta_1/\eta_2$ Trendlines

Figure 3-24: $\eta_3/\eta_4$ Trendlines
\[ \delta \eta = \eta_3 - \eta_4 \]

\[ \delta \eta_{l_{\min}} = 0.03 \]

\[ l_{\text{mean}} = 0.16 \]

\[ l_{\max} = 0.29 \]

**Figure 3-25: \( \delta \eta \) Trendlines**

**Figure 3-26: Schematic for \( Z^{-2} \) Proof**
3.3 Discussion

It is clear that the values of impulse are much lower for a finite surface than for an infinite surface. Examination of the presented figures, along with equations (3-5) through (3-15) enables the following observations.

Firstly, examination of Figures 3-15 through 3-18 suggests that the effect of scaled flange width is modest in comparison to the effect of scaled distance, merely increasing the scatter in the results. The trendlines for measures 1 through 4 shown in Figures 3-8 through 3-11 support this observation by demonstrating that, in general, the scatter of the observed values of impulse are bounded by the maximum and minimum scaled flange width for all measures.

Secondly, the rate of decay of impulse with scaled distance, when accounting for wrap-around effects (measures 3 and 4) is much higher than that of the HC curve and measures 1 and 2. This can be observed by considering the slope of the trendlines in Figures 3-15 through 3-18 and from equations (3-5) through (3-18). As mentioned in section 3.1.2, the regression parameters represent the slope of the line when plotted on a log scale. Consider equations (3-5) through (3-18). The equations suggest that when wrap-around is considered the impulse is approximately proportional to $Z^{-2}$, that is, impulse is proportional to the inverse of the scaled distance squared. For infinite surfaces, the impulse is proportional to $Z^{-1}$, thus, on a log-log scale the impulse decays twice as rapidly when the section dimensions are finite.

This observation implies that, for sections which can be considered finite, as scaled distance increases the value of impulse decays rapidly and is substantially lower than the impulse for an infinite section at the same scaled distance. A physical interpretation of this observation is related to the relationship of reflection coefficient and scaled distance. As scaled distance becomes large, the reflection coefficient tends toward 2 in the absence of clearing according to Figure 1.6 with $\alpha = 0$. It was demonstrated in Appendix B that the time taken for the front face to clear from a reflected pressure to a side-on pressure is a fraction of the loading duration for typical W-shape sections, resulting in the front-face pressures having similar orders of magnitude as the rear-face pressures. If the pressures experienced by the rear face of the W-shape section
are considered ‘canceling’ pressures, at large scaled distances the canceling pressures are approximately equal to the reflected pressures, resulting in a very large percentage reduction in the impulse. A mathematical proof is presented below.

Consider Figure 3-12, a rectangular object of scaled dimensions \( b \times d \) with front surface located at a scaled distance \( Z \) from a point source. From equation (3-5), the side-on impulse on the front face is approximately;

\[
I_1 \propto \frac{1}{Z} \quad (3-18)
\]

and on the back face is

\[
I_2 \propto \frac{1}{Z + d} \quad (3-19)
\]

The net impulse on the section is approximately;

\[
I_1 - I_2 \propto \frac{1}{Z} - \frac{1}{Z + d} \quad (3-20a)
\]

\[
I_1 - I_2 \propto \frac{1}{Z} \left(1 - \frac{Z}{Z + d}\right) \quad (3-20b)
\]

By performing a Taylor series expansion of the fraction within brackets in equation (3-20b) and truncating after the second term, it is possible to write the net impulse as;

\[
I_1 - I_2 \propto \frac{1}{Z} \left(1 - \left(1 + \frac{-d}{Z}\right)\right) \quad (3-20c)
\]

\[
I_1 - I_2 \propto \frac{d}{Z^2} \quad (3-20d)
\]
For the proof to be valid $b << Z$ and $d << Z$ must be satisfied, which for most member sections and threats will be the case.

The final observation is that the main benefit of encasing a W-shape section or filling the voids between the flanges of a W-shape section is at scaled distances lower than $10 \text{m/}\sqrt{\text{kg}}$ as although the ratio of $\eta_3$ to $\eta_4$ increases with increasing $Z$, at $Z > 10 \text{m/}\sqrt{\text{kg}}$, $\eta_4$ is already less than 0.05. Surprisingly, the shape or scaled width of the section has a minimal effect on impulse if compared to the effect of scaled distance, provided that the section is finite.
SECTION 4
CONCLUSION

4.1 Introduction

In general, current design procedures for blast loading involve application of simplified SDOF procedures to member design. Two distinct approaches exist depending upon the dynamic properties of the system. For members (or structural systems) whose natural period of response is of similar magnitude or smaller than the loading duration, a quasi-static approach is utilized whereby the wave reflected pressures are the critical loading parameter. Alternatively, for members (structural systems) whose natural period is much greater than the loading duration, initial conditions can be derived based upon the impulse imparted on the system by the blast wave. Blast wave pressure histories can be defined using four key parameters: arrival time, load duration, peak pressure and reflected impulse. Empirical relationships (HC curves) defining these parameters were derived from experimental data but are generally applicable to reflective surfaces that are infinite in size. This is primarily a result of the research at that time being focused on the effects of atomic and nuclear weapons. However, for the situation where conventional and improvised explosives are being used and individual members of structural systems are being analyzed and designed, the reflective surfaces are far from infinite.

The goal of this work was to investigate whether reductions in impulse could be observed due to the finite dimensions of a structural section. Prior to the study, two main mechanisms were proposed that could potentially lower the impulse imparted on the member: clearing and wrap-around. The conclusions of the study are presented below.

4.2 Conclusions

The main conclusions of the analytical studies described above are;

- When a section can be considered finite, the impulse is approximately proportional to $Z^{-2}$ rather than $Z^{-1}$ that applies for an infinite surface. This effect is primarily due to the wrapping of the blast wave around the cross section although there is a contribution from clearing. The consequence of this result is that as $Z$ increases, the impulse
decreases rapidly, allowing a structural member to be designed for a much smaller impulse.

- The reduction in scaled impulse due to clearing is approximately constant at 50% for the range of scaled distance and scaled flange width considered in the study.

- The effect of section width is small when compared to the effect of scaled distance, provided the section width is small enough for the section to be considered ‘finite’. In this study, a typical depth-to-breadth ratio of 1.1 was assumed thus the effect of section depth could not be examined in a detailed manner. However, provided that depth is small enough to be considered ‘finite’ the effect is most likely minimal.

- The effect of the chosen structural shape appears small when compared to the effect of scaled distance and the plan dimensions of the section can be considered to be finite. Being open or closed does not alter the scaled impulse on a section significantly if compared to the effect of the section being regarded as finite. However, at scaled distances below $10m/\sqrt{kg}$, the influence of the structural shape becomes more important than at scaled distances greater than $10m/3\sqrt{kg}$.

### 4.3 Recommendations

As with most developments, further work is required to substantiate and refine the conclusions. This study identified that reflected impulse is heavily influenced by the cross-section size (finite or infinite) but additional studies are required. A discussion of further work and recommendations is contained below.

Firstly, the effect of section orientation has not been investigated as all cases in this study involved sections whose front surface was tangent to the shock front. A section which is loaded at an oblique angle may be more sensitive to the structural shape.

Furthermore, the conclusions of the report whilst being generally applicable will most likely breakdown in certain regimes. For example, at what scaled width and depth can a section be considered ‘finite’ or the range of scaled distance at which the structural shape has more influence on the results? Identification of such regimes is an important next step.
Further work to confirm the $3S/U$ calculation of clearing time (developed for atomic weapons effects) for conventional high explosives would enable use of the derivations and calculations, presented in manuals, in the open literature.

In addition, the rigid material assumption should be investigated further if only to gain additional confidence in the assumption. This, however, is not a simple task and would require highly complicated numerical analysis that can robustly deal with material non-linearity and fluid-structure interaction. The main restriction on this type of work is material modeling of structural grade steel in these types of applications (this restriction in itself represents a significant academic challenge).

We used Air3d extensively for this study. Although Air3d is specifically intended for air-blast calculations, some additional features would be most useful. During the solution process, the software only provides pressure and temperature data. Access to the velocity components for the entire domain would greatly help in visualizing and interpreting results. In Air3d, the whole domain from burst point to section (and more) has to be solved for every analysis. Significant computational effort is spent solving for cells that do not yield information of ongoing use. An alternative approach would be to use computational fluid dynamics (CFD), which could offer a number of benefits. CFD calculates the coupled velocity and pressure fields involved in fluid dynamics and can therefore provide additional information about the scenario. In solving the coupled velocity and pressure fields more computational effort per timestep is required. However, this increase can be offset by CFD’s ability to only model the local domain around the structural shape, dramatically reducing the number of cells in the model. Another benefit of CFD is that most of the current commercial codes provide a framework for some level of fluid-structure interaction, an area which has already been identified as needing further work. The final benefit of a CFD approach is that the post processing features would allow much more detailed visualization of the solved variables resulting in better understanding of the flow around the section.

Finally, and most importantly, the analytical results from this study from Air3d have no physical data to be compared to although it has been benchmarked against some forms of blast data.
CFD has even less validation in the field of blast wave propagation and supporting physical experiments are crucial before claims on the predicted reductions are made by the engineering community.
SECTION 5

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APPENDIX A
FACTORIAL DESIGN

A.1 Introduction
The concept of factorial design was introduced in Chapter 2, however, lengthy discussions and cumbersome examples were avoided to improve the readability of the report. This appendix provides more detail of factorial designs through discussion of the advantages and a worked example.

A.2 Advantage of Factorials
There are three main advantages in factorial design, namely 1) they are more efficient than one-factor-at-a-time (OFAT) experiments, 2) factorial designs allow estimation of the interaction of factors, and 3) after interaction effects have been captured, then the influence of a factor at several levels of the other factors can be estimated, improving the robustness of the conclusions. Each of these advantages is explained in more detail below.

A.3 Efficiency
Typically in experimentation, OFAT experiments are used where only one variable or factor is varied and the others held constant. Factorial designs only ever have two or three levels, therefore only require $2^k$ or $3^k$ experiments (where 2 or 3 is the number of levels and k is the number of factors). The improvement in efficiency comes from the fact that in general, fewer factor levels are required to obtain the same level of information.

A.4 Interaction Effects
The second advantage of factorial designs is that the interaction between factors can be captured. For example, if we say $y$ is a function of the factors (variables) $A$, $B$ and $C$ such that $y = f(A, B, C)$ and that factors take on two levels $(A_1, A_2, B_1, B_2, C_1, C_2)$. When interaction effects are not present, then the change in $y$ by changing from $A_1$ to $A_2$ is unaffected by the relative value of the factors (the change in response by changing a factor is called the ‘main effect’ of that factor). When interaction is present, the change in $y$ is dependant upon the level of factors $B$ and $C$. That is, when factor $B$ is at level $B_1$, changing from $A_1$ to $A_2$
may cause an increase in $y$, however, when level $B$ is at $B_2$ the same change from $A_1$ to $A_2$ may cause a reduction in $y$ (this change in response is called the ‘interaction effect’ of those factors). It is this type of interaction that factorial designs can capture and OFAT experiments cannot. The significance of this is that wrong conclusions may be drawn based upon an OFAT experiment in which interaction is present, particularly when the interaction effect causes a change in the response that is of a similar order as the main effect.

### A.5 Improved Robustness

Often in experimentation, linear regression is performed upon the data to be able to interpolate for factor levels (variable values) that were not examined in the actual experiments. The danger of not capturing interaction effects is that the linear regression model is not being fitted to the appropriate data and cannot predict any existing interaction, leading to regression results that are unreliable at best and useless at worst. By using factorial designs, it is possible to capture interaction of factors and therefore generate a more reliable and robust regression model that can be confidently used to interpolate between the factor levels.

### A.6 Worked Example

A worked example taken from Montgomery (1991) to illustrate the effect of interaction is shown below. Let the main effect be the difference between the average responses at the different levels, thus there can be a main effect for each factor.

Consider the two data sets in Table A-1 for an experiment without interaction and with interaction, where $A$ and $B$ are factors in the response of $Y$. For data set $I$, the main effect of $A$ is

$$A_I = \frac{40 + 52}{2} - \frac{20 + 30}{2} = 21$$

where the first term is the average response of $Y$ with $A$ at level 2 and the second term is the average response of $Y$ with $A$ at level 1. Increasing factor $A$ from level 1 to level 2 increases the average response by 21 units. Similarly for factor $B$, the main effect is
When the difference in response is not the same at all levels, interaction is said to exist. Consider data set II, at the first level of \( B \), the \( A \) effect is

\[
A_{B_1} = 50 - 20 = 30 \tag{A-3}
\]

and at the second level of factor \( B \), the \( A \) effect is

\[
A_{B_2} = 12 - 40 = -28 \tag{A-4}
\]

Clearly from equations (A-3) and (A-4) the effect of \( A \) is not the same at the two levels of \( B \). This suggests interaction between \( A \) and \( B \). The main effect of \( A \) in this example is

\[
A_I = \frac{50 + 12}{2} - \frac{20 + 40}{2} = 1 \tag{A-5}
\]

Since the main effect of \( A \) is small, it suggests that there is minimal effect on the average response due to \( A \), however, in the presence of significant interaction ‘main effects’ can be dwarfed by ‘interaction effects’. Figure A-1 and A-2 show plots of response against factor for both data sets I and II. In Figure A-1 shows that the lines for factor \( B \) at levels I and II run parallel, demonstrating little or no interaction, while Figure A-2 shows the lines are not parallel. Clearly the ability to capture interaction effects is important.
# Table A-1: Sample Data Sets

<table>
<thead>
<tr>
<th></th>
<th>Data set I – no interaction</th>
<th>Data set II – with interaction</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>B₁</td>
<td>B₂</td>
</tr>
<tr>
<td>A₁</td>
<td>20</td>
<td>30</td>
</tr>
<tr>
<td>A₂</td>
<td>40</td>
<td>52</td>
</tr>
</tbody>
</table>

![Figure A-1: Response Plot for Data Set I](image)

**Figure A-1: Response Plot for Data Set I**
Figure A-2: Response plot for data set II
APPENDIX B
AIR3D VALIDATION

B.1 Introduction
Although Air3d was validated against the HC curves for side-on and reflected pressure and impulses in Chapter 2, further validation is required to have confidence in the results of the study.

Each of the four measures, defined in Chapter 3, is interrogated in detail for a selected combination of $R = 6.63\text{m}$, $m_{int} = 14.6\text{kg}$ and $b_f = 0.459\text{m}$. The measures are treated in sequential order, beginning with Measure 1.

B.2 Measure 1
Measure 1 is defined as the impulse at the 1st monitoring point (located on the front face of the front flange, closest to the web centerline). In the absence of clearing, the impulse returned for measure 1 should match exactly with CONWEP and the HC curves. Table B-1 below shows data for measure 1 from Run 5 where $R = 6.63\text{m}$, $m_{int} = 14.6\text{kg}$, $Z = 2.71\text{m}/\sqrt{\text{kg}}$ and $b_f = 0.459\text{m}$.

Firstly, consider the values of $r_P$ in Table B-1; HC, CONWEP and Air3d all predict a very similar value for reflected pressure. This is an expected result because peak reflected pressure is not affected by clearing. Similarly, the three values of $t_a$ are most similar. For reflected impulse, $i^*_r$, HC and CONWEP are within 20% of each other, but the Air3d result is approximately 50% of the HC and CONWEP values. Norris (1959) proposed that the time taken for the reflected pressure to clear a surface can be approximated as;

$$t_c = \frac{3S}{U}$$  \hspace{1cm} (B-1)
where $t_c$ is the clearing time, $S$ is the distance from the nearest free edge to the point of interest and $U$ is the shockwave velocity. For Run 5 (see Table 2-4), $S = b_f / 2 = 0.23\text{m}$ and $U = 463\text{m/s}$. From equation (B-1) the time to clear the entire front face of the flange is;

$$t_c = \frac{3 \times 0.23}{463} = 1.49 \times 10^{-3} \text{s}$$

(B-2)

The ratio of the clearing time to the CONWEP load duration, $t_c / t_d = 0.24$. This suggests that the reflected pressure has decayed to the cleared pressure in 24% of the positive phase duration (the cleared pressure is the sum of the side-on pressure and the dynamic drag pressure, for this example the peak dynamic pressure is approximately one-third of the peak side-on pressure). Here, the effect of clearing is felt across the entire front face of the flange.

The example was re-analyzed to confirm that clearing causes the shown reduction in reflected impulse. By extending the width of the W-shape to the entire domain width and holding all other analysis input at the Run 5 values, the effect of clearing was isolated. The last column in Table B-1 presents the results of this analysis. The reflected pressure and arrival time are identical for the Air3d results, as would be expected. The reflected impulse agrees very well with CONWEP and to a lesser degree the HC value, confirming that the reduction in measure 1 is solely due to clearing. Although the Air3d reflected impulse for the infinite surface is 20% lower than the HC value, this is consistent with the discussion of Air3d’s validation against the HC data in Chapter 2 which showed that for $Z > 2$, Air3d predicted a value of impulse approximately 20% lower than HC curves.
B.3 Measure 2

Measure 2 represents the area-averaged impulse across the front face of the front flange. The ability of Air3d to predict clearing was confirmed while validating measure 1. Examination of Figures 3-8 and 3-9 suggests that measure 1 and 2 give the exact same reduction in impulse. Since the effect of clearing would be greater at the extremities of the flange, one would expect measure 2 to be less than measure 1. Table B-2 shows the values of impulse and the distance from the web centerline for the 12 monitoring locations in Region 1, for Run 5. As one would expect, the impulse at the outermost monitoring location (point 12) is the minimum (increased standoff and clearing) and the impulse at the innermost monitoring location is the maximum (point 1). Figure B-1 plots the actual impulse distribution along region 1 with respect to distance from the web centerline and the numeric average impulse. The distribution is plausible with the average impulse on region 1 being 95% of the maximum (206/218 = 0.95). Measure 2 is very close to measure 1 and the difference is difficult to identify when results are plotted on a log scale. This outcome is supported by Figure 3-12, which plots the ratio of measure 1 to measure 2. At a scaled distance of \( Z = 2.71 \text{m}/\sqrt{\text{kg}} \) the ratio is 1.07, which is approximately equal to the inverse of 0.95. This example validates the reported results for measure 2.

<table>
<thead>
<tr>
<th>Variable</th>
<th>HC</th>
<th>CONWEP</th>
<th>Air3d</th>
<th>Air3d (Ext. flanges)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( P_i ) (kPa)</td>
<td>281.50</td>
<td>278.9</td>
<td>259.5</td>
<td>259.5</td>
</tr>
<tr>
<td>( i^+ ) (kPa-msec)</td>
<td>491.9</td>
<td>403.0</td>
<td>218.0</td>
<td>401.9</td>
</tr>
<tr>
<td>( t_a ) (msec)</td>
<td>7.58</td>
<td>8.20</td>
<td>8.19</td>
<td>8.19</td>
</tr>
<tr>
<td>( t_d ) (msec)</td>
<td>5.87</td>
<td>6.16</td>
<td>3.90</td>
<td>4.91</td>
</tr>
</tbody>
</table>

Table B-1: Measure 1 Validation

(\( R = 6.63 \text{m} \), \( m_{nt} = 14.6 \text{kg} \), and \( b_f = 0.459 \text{m} \))
Table B-2: Impulse and Distance from Centerline for Monitoring Locations

\[ R = 6.63 \text{m}, \ m_{\text{int}} = 14.6 \text{kg}, \text{ and } b_f = 0.459 \text{m} \]

<table>
<thead>
<tr>
<th>Mon. loc.</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
<th>12</th>
</tr>
</thead>
<tbody>
<tr>
<td>( x ) (mm)</td>
<td>9.00</td>
<td>18.3</td>
<td>39.5</td>
<td>60.6</td>
<td>81.7</td>
<td>102</td>
<td>124</td>
<td>145</td>
<td>166</td>
<td>187</td>
<td>209</td>
<td>230</td>
</tr>
<tr>
<td>( i_r^+ ) (kPa-msec)</td>
<td>218</td>
<td>218</td>
<td>218</td>
<td>217</td>
<td>215</td>
<td>213</td>
<td>211</td>
<td>207</td>
<td>203</td>
<td>198</td>
<td>187</td>
<td>170</td>
</tr>
</tbody>
</table>

1. For monitoring locations, see Figure 2-2 and Section 2.1

**Figure B-1:** Region 1 Impulse Distribution \( R = 6.63 \text{m}, m_{\text{int}} = 14.6 \text{kg}, \text{ and } b_f = 0.459 \text{m} \)

**B.4 Measure 3 and 4**

Measures 3 and 4 are intended to capture the effect of wrap-around by combining the impulses for regions 1 through 4 based upon their surface normals. The impulse on each region is determined by integrating the area-averaged pressure history for that region. An area-average was used because 2 monitoring locations lie on the flange surface over the web and 10 monitoring locations lie on the remainder of the flange, resulting in points 1, 2, 43 and 44 having...
a different tributary area than the other monitoring locations. However, examination of Table B-3 reveals that the variation in impulse between points 1 and 2 is negligible and similarly for points 33 and 34. Therefore, the error introduced by approximating the individual region impulse as the numeric average of the monitoring location impulse within the regions is small. Measures 3 and 4 are examined on this basis.

From the data in Table B-3, the reflected impulses on regions 1, 2, 3 and 4 are 206kPa-msec, 135kPa-msec, 177kPa-msec and 131kPa-msec, respectively. Review of these values reveals a logical pattern; Region 1 has the largest value since it is the closest to the charge and is a reflective surface. Region 2 values are smaller since it experiences a side-on pressure. Region 3 experiences a reflected wave and thus has a larger impulse than region 2 but smaller impulse than region 1 as it is further from the charge. Region 4 has the smallest value as it experiences a side-on pressure and is furthest from the charge. Comparison of region 1 and 3 suggests that region 4 is too close to the region 3 value of impulse. Examination of the points 33 – 44 in Table B-3 reveal that points 33 and 34 take an unexpected jump to a value of almost twice point 35. This can be explained by considering the behavior of a wave as it propagates around a W-shape. As the wave strikes the section, the flow splits equally around the section (since the section is symmetric), the waves engulf the front flange and then the rear flange before the waves re-engage at the web centerline. The passage of the waves past one another on the rear face of
the rear flange increases the side-on pressure and impulse above that associated with one wave only.

Measure 3 has been defined as the summation of regions 1 through 4, with regions 1 and 3 being additive and regions 2 and 4 being subtractive. This implies that the measure 3 value of scaled impulse is;

\[
\frac{206 - 135 + 177 - 131}{\sqrt[3]{14.6}} = 47.8 \text{ kPa} \cdot \text{msec} \sqrt[3]{\text{kg}} \quad \text{(B-3)}
\]

Figure 3-10 for \( Z = 2.71 \sqrt[3]{\text{m/kg}} \) suggests that the measure 3 scaled impulse is approximately 50 kPa \cdot \text{msec} / \sqrt[3]{\text{kg}} , which indicates that the simplified numerical approach agrees very well with the area-average method. Measure 4 was intended to represent a tubular section (rectangular hollow section, RHS) with the same outer dimensions as the W-shape of measure 3 and was defined as region 1 – region 4, the value of impulse based on Table B-3 is;

\[
\frac{206 - 131}{\sqrt[3]{14.6}} = 30.6 \text{ kPa} \cdot \text{msec} \sqrt[3]{\text{kg}} \quad \text{(B-4)}
\]

The measure 4 scaled impulse from Figure 3-11 for \( Z = 2.71 \sqrt[3]{\text{m/kg}} \) is 30 kPa \cdot \text{msec} / \sqrt[3]{\text{kg}} , again agreeing very well with the area-average method. The HC value of scaled impulse is 200 kPa \cdot \text{msec} / \sqrt[3]{\text{kg}} . Thus even at relatively small scaled distances (\( Z = 2.71 \sqrt[3]{\text{m/kg}} \) ), a 4 and 7 fold reduction in scaled impulse is realized from measure 3 and 4 respectively.

In addition to the above validation of measure 4, it is necessary to demonstrate that the impulse for region 4 of a W-shape is very similar to that of a RHS with the same outer dimensions, which would validate the assumption that (region 1 – region 4) returns the net impulse on a RHS shape. Six additional analyses (B1 through B6) were performed in order to validate this assumption, using three W-shapes and three tubular sections. The analysis details were \( R = 2.44, 6.63 \) and \( 12.22 \text{m}, m_{\text{int}} = 14.6 \text{kg} \), and \( b_f = 0.459 \text{m} \) which corresponds to \( Z = 1, 2.71 \) and \( 5 \sqrt[3]{\text{m/kg}} \).
Table B-4 shows the values of impulse at each of the monitoring locations for analyses B1 through B6. The average impulse for region 4 for B1 through B6 is 607, 589, 131, 129, 41 and 42 kPa-msec respectively. The percentage difference is calculated below;

\[
\left(1 - \frac{i_{B1}^+}{i_{B2}^+}\right) \times 100 = \left(1 - \frac{607}{589}\right) \times 100 = -3% \quad \text{(B-5)}
\]

\[
\left(1 - \frac{i_{B3}^+}{i_{B4}^+}\right) \times 100 = \left(1 - \frac{131}{129}\right) \times 100 = -2% \quad \text{(B-6)}
\]

\[
\left(1 - \frac{i_{B5}^+}{i_{B6}^+}\right) \times 100 = \left(1 - \frac{41}{42}\right) \times 100 = 2% \quad \text{(B-7)}
\]

It is clear from equations (B-5) through (B-7) that the region 4 impulse of a W-shape is essentially unaffected by regions 2 and 3, therefore ignoring regions 2 and 3 allows a most reasonable estimate of the net impulse on a RHS with the same outer dimensions.

### B.5 Summary

Given the complicated nature of blast loading, exact solutions are rare which makes validation of numerical results difficult, however, the requirement of validation still exists. Using HC curves and CONWEP, the values generated by Air3d were validated. The trends predicted in Chapter 3 have been interrogated, justified and approximated using simplified, transparent procedures that agreed well with the data in Chapter 3.
Table B-4: Impulse at each Monitoring Location in Region 4

Run B1: W-shape \( (R = 2.44\text{m}, m_{int} = 14.6\text{kg}, \text{ and } b_f = 0.459\text{m}) \)

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<th>Mon. loc.</th>
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<th>44</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i_r^+ ) (kPa-msec)</td>
<td>825</td>
<td>850</td>
<td>8</td>
<td>432</td>
<td>482</td>
<td>529</td>
<td>578</td>
<td>637</td>
<td>676</td>
<td>720</td>
<td>752</td>
<td>798</td>
</tr>
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</table>

Run B2: RHS \( (R = 2.44\text{m}, m_{int} = 14.6\text{kg}, \text{ and } b_f = 0.459\text{m}) \)

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<th>44</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i_r^+ ) (kPa-msec)</td>
<td>799</td>
<td>820</td>
<td>7</td>
<td>441</td>
<td>471</td>
<td>510</td>
<td>555</td>
<td>615</td>
<td>654</td>
<td>699</td>
<td>730</td>
<td>773</td>
</tr>
</tbody>
</table>

Run B3: W-shape \( (R = 6.63\text{m}, m_{int} = 14.6\text{kg}, \text{ and } b_f = 0.459\text{m}) \)

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<tbody>
<tr>
<td>( i_r^+ ) (kPa-msec)</td>
<td>149</td>
<td>149</td>
<td>76</td>
<td>91</td>
<td>117</td>
<td>130</td>
<td>137</td>
<td>141</td>
<td>143</td>
<td>145</td>
<td>146</td>
<td>148</td>
</tr>
</tbody>
</table>

Run B4: RHS \( (R = 6.63\text{m}, m_{int} = 14.6\text{kg}, \text{ and } b_f = 0.459\text{m}) \)

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<th>44</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i_r^+ ) (kPa-msec)</td>
<td>145</td>
<td>145</td>
<td>92</td>
<td>89</td>
<td>109</td>
<td>123</td>
<td>132</td>
<td>139</td>
<td>142</td>
<td>145</td>
<td>146</td>
<td>144</td>
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</tbody>
</table>

Run B5: W-shape \( (R = 12.2\text{m}, m_{int} = 14.6\text{kg}, \text{ and } b_f = 0.459\text{m}) \)

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<tr>
<td>( i_r^+ ) (kPa-msec)</td>
<td>43</td>
<td>43</td>
<td>33</td>
<td>37</td>
<td>40</td>
<td>41</td>
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Run B6: RHS \( (R = 12.2\text{m}, m_{int} = 14.6\text{kg}, \text{ and } b_f = 0.459\text{m}) \)

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<tr>
<td>( i_r^+ ) (kPa-msec)</td>
<td>44</td>
<td>44</td>
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<td>41</td>
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1. For monitoring locations, see Figure 2-2 and Section 2.1
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<th>Dates</th>
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<td>D.C.K. Chen and L.D. Lutes</td>
<td>9/19/88,</td>
<td>PB89-131437, A04, MF-A01</td>
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<td>A.M. Reinhorn, S.K. Kunnath and N. Panahshahi</td>
<td>9/7/88,</td>
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<td>G.W. Ellis and A.S. Cakmak</td>
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